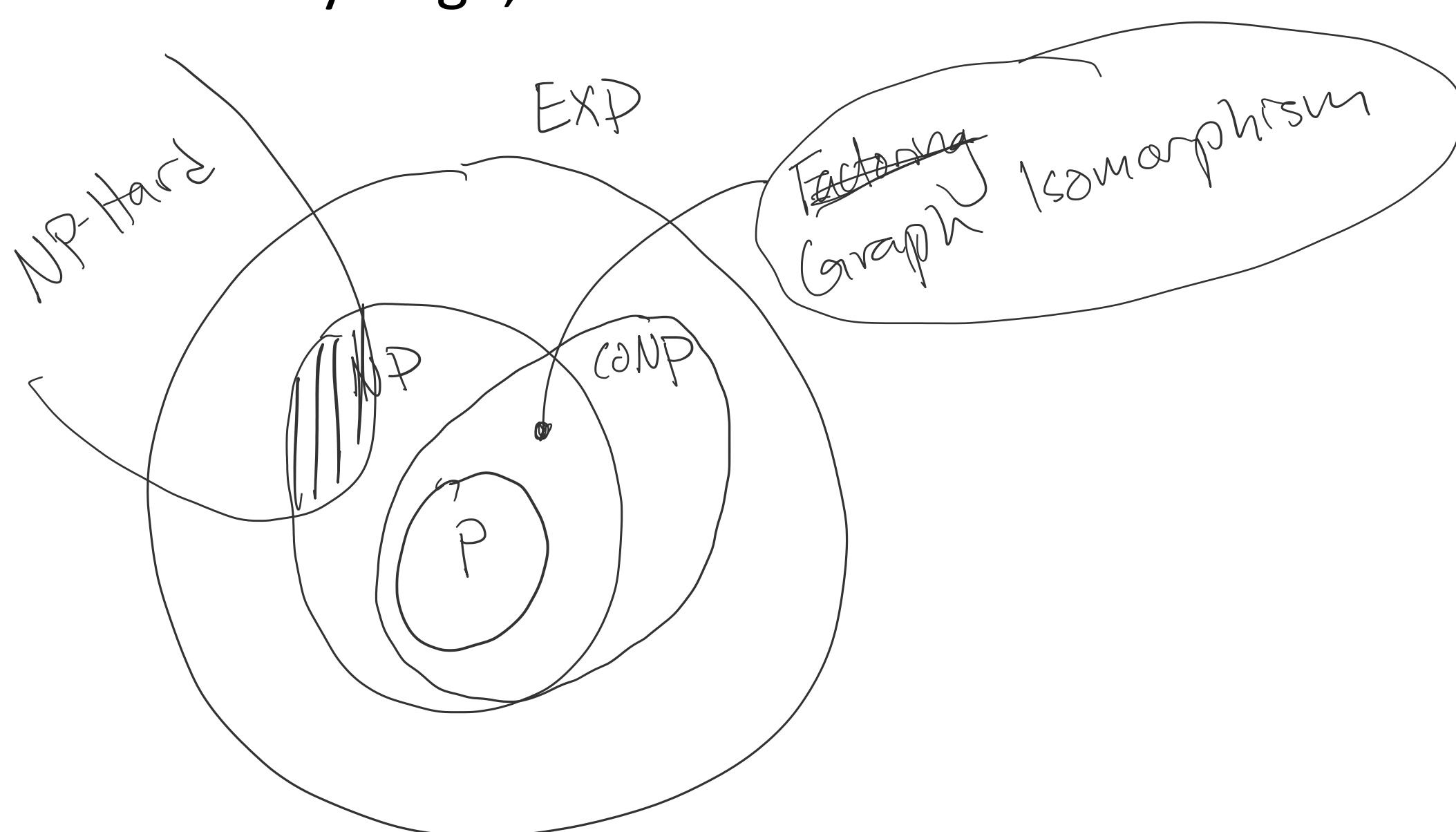


- Where is coNP in our picture?
- For any finite sized language in NP, the complement of that language will be infinitely large, which doesn't seem useful.



$$\underline{P \subseteq \text{coNP}}$$

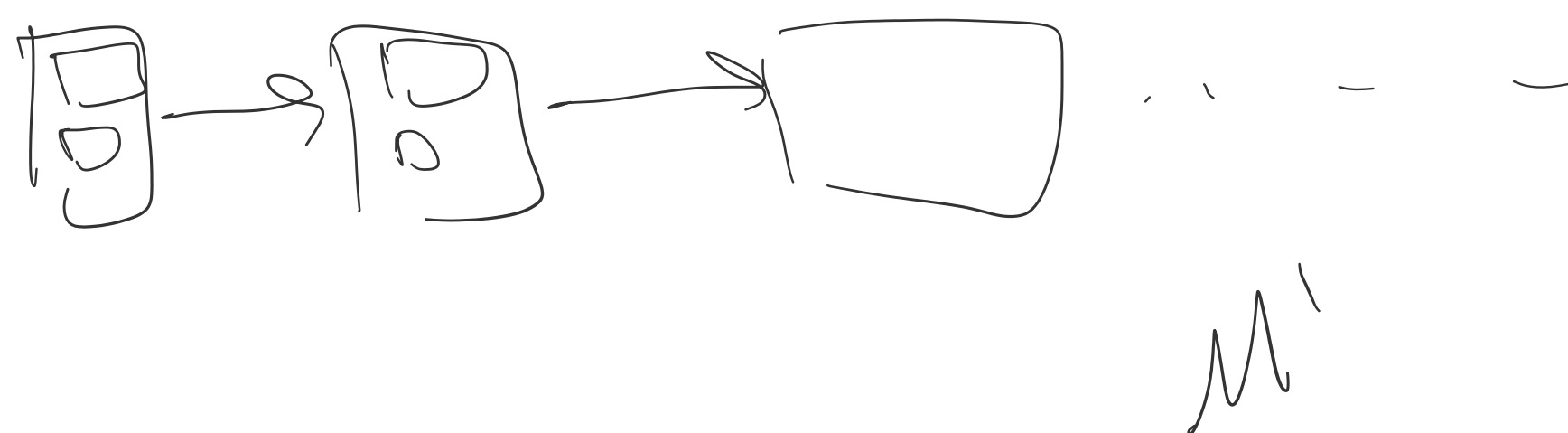
$$\text{coNP} \subseteq \text{EXP}$$

$L \in P$ .  $\exists$  a polytime TM such that  $M(x) = 1$  iff  $x \in L$ . Consider TM  $M'$ , that outputs the opposite of  $M$  ( $q_{\text{accept}} \leftrightarrow q_{\text{reject}}$ ).  $M'$  decides  $\bar{L}$ , therefore  $\bar{L} \in P$ . Thus  $\bar{L} \in \text{NP}$ . So  $L \in \text{coNP}$ .

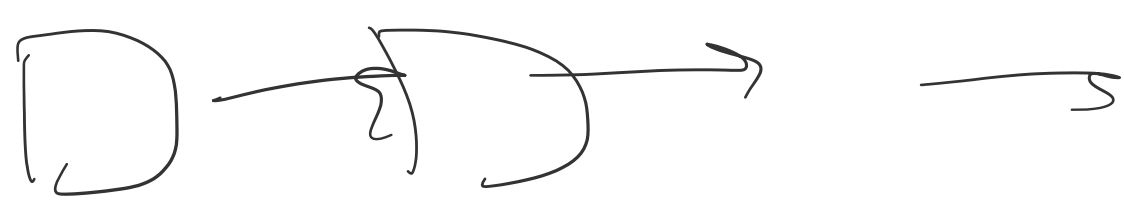
$L \in \text{coNP}$ . Then  $\bar{L} \in \text{NP}$ . Then  $\bar{L} \in \text{EXP} \Rightarrow L \in \text{EXP}$

$\exists$  exponential time TM  $M$  that decides  $\bar{L}$ . Consider  $M'$  that acts like  $M$  but exchanges  $q_{\text{accept}} \leftrightarrow q_{\text{reject}}$

$M'$  decides  $L$ .



$q_{\text{accept}}$



$q_{\text{reject}}$