

## 4s. Reductions

Monday, February 21, 2022 11:24 AM

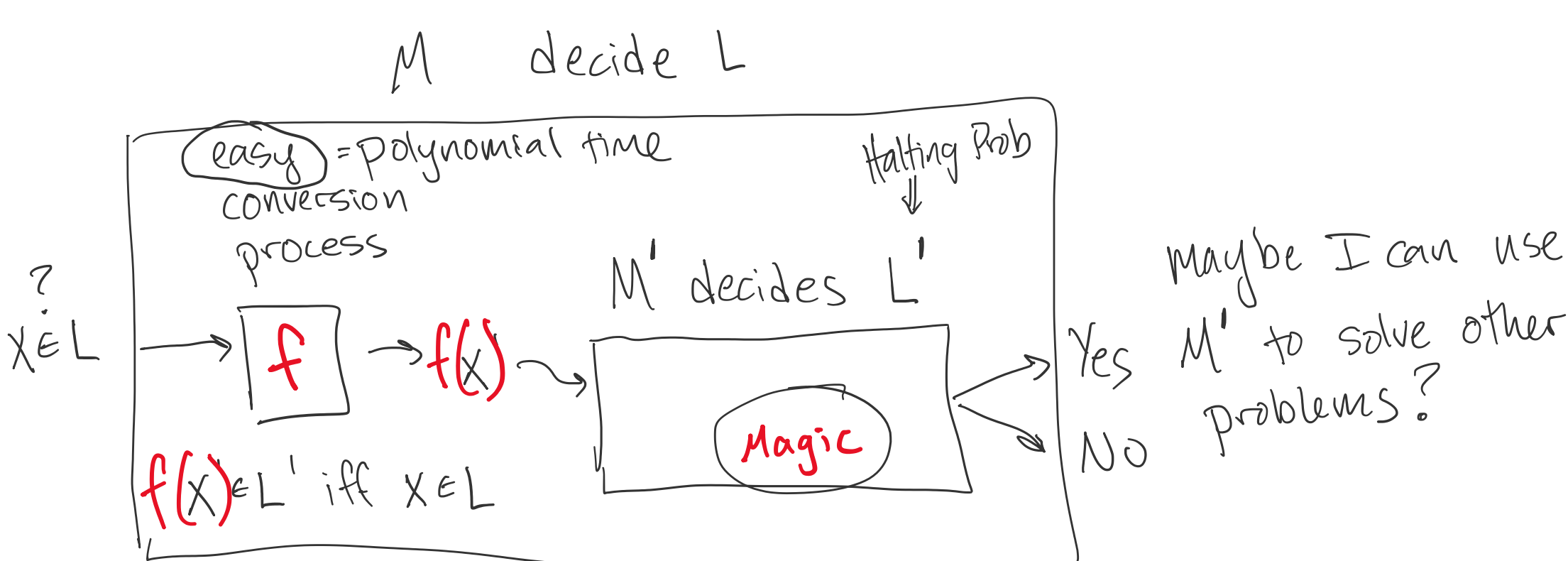
### Goals

- Describe how we use reductions to compare problems
- Write a proof using reductions.

### What is Computational Complexity?

- What resources are required to solve a problem? ~~← Hard~~
- What is the relative power of computational resources? ~~←~~
- What is the relative difficulty of solving various problems ~~← Easier~~

Addition vs. Multipl. vs. Trav. Sales



Resources needed to solve  $L'$  are sufficient to solve  $L$ . (Might be way more than needed)

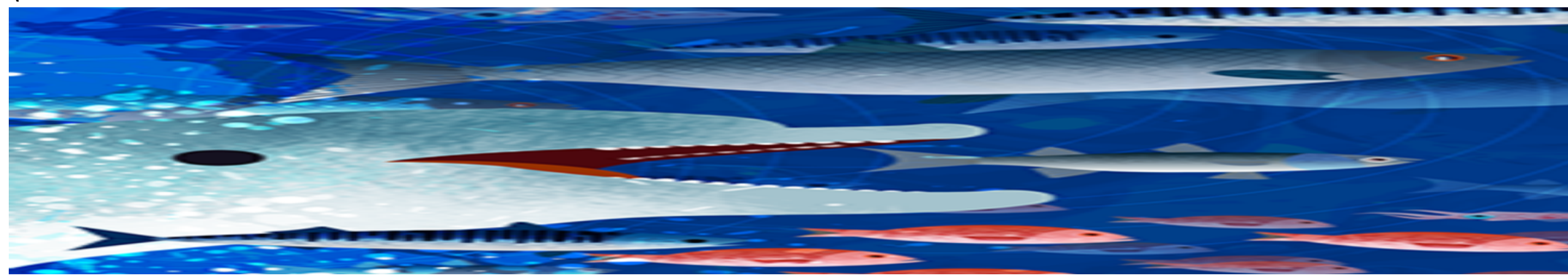
" $L'$  is harder than  $L$ "

### Reductions

A language  $L \subseteq \{0,1\}^*$  is polynomial time reducible to  $L' \subseteq \{0,1\}^*$ , denoted  $L \leq_p L'$ , if there is a polynomial-time computable function  $f: \{0,1\}^* \rightarrow \{0,1\}^*$  s.t.  $\forall x \in \{0,1\}^*, x \in L \text{ iff } f(x) \in L'$ .

$\downarrow O(n^d)$  for some  $d \geq 1$ .

Prove: If  $L' \in P$  and  $L \leq_p L'$ , then  $L \in P$



Let  $M$  be the TM that does [ ~ ]

Then  $M(x) = 1$  iff  $x \in L$  b/c [ ~ ]

Now  $M$  runs in  $O(n^{??})$  steps b/c [ ~ ]

