

# Greedy Scheduling

If we get rid of the assumption that all  $w_i/t_i$  are unique, what changes? Which change(s) make the proof fail?

# Knapsack

- If  $S$  is optimal solution to  $K_{n,W}$ , and  $n \notin S$ , then \_\_\_\_\_ is optimal solution to  $K_{-, -}$
- If  $S$  is optimal solution to  $K_{n,W}$ , and  $n \in S$ , then \_\_\_\_\_ is optimal solution to  $K_{-, -}$
- Prove each statement. Start: For contradiction, assume \_\_\_\_\_ is not optimal solution to  $K_{-, -}$

# Knapsack

- If  $S$  is optimal solution to  $K_{n,W}$ , and  $n \notin S$ , then  $S$  is optimal solution to  $K_{n-1,W}$
- If  $S$  is optimal solution to  $K_{n,W}$ , and  $n \in S$ , then  $S - \{n\}$  is optimal solution to  $K_{n-1,W-w_n}$

# Knapsack

- If  $S$  is optimal solution to  $K_{n,W}$ , and  $n \in S$ , then  $S - \{n\}$  is optimal solution to  $K_{n-1, W-w_n}$

Suppose for contradiction  $S - \{n\}$  is not the optimal solution to  $K_{n-1, W-w_n}$ . Then the optimal solution  $S'$  to  $K_{n-1, W-w_n}$  has  $V(S') > V(S - \{n\})$ . But then  $S' \cup \{n\}$  is a solution to  $K_{n,W}$  with  $V(S' \cup \{n\}) > V(S)$ , so  $S$  is not optimal for  $K_{n,W}$ , a contradiction.