Proof By Cases

Use a proof by cases to show:

For any integer n, the number $n^3 - n$ is even.

If finish, please sit and work on:
If k is a multiple of 4, then $\exists n \in \mathbb{N}$:

$$k = 1 + (-1)^n(2n - 1)$$