

Suppose you run algorithm twice and get c, c' both good, and get approximations $\frac{a}{b}, \frac{a'}{b'}$ then prob. $\text{LCM}(b, b') = r$ is $\frac{1}{2}$.

Time Complexity of factoring Comparison to Classical

N is size of domain of f
 $\Leftrightarrow N$ is # to factor

- $QFT_N: O((\log_2 N)^2)$ single + 2 qubit gates
- U_f : For factoring application: $O(\log_2 N)$ gates

$\Rightarrow O((\log_2 N)^2)$ time for Quantum

$\Rightarrow e^{O((\log_2 N)^{1/3})}$ for classical
"number field sieve"

↓
Sub-exponential in $\log_2 N$ (almost exponential)

↓
polynomial in $\log_2 N$