CS333 - Qubit Worksheet

- 1. If you measure the state $|\psi\rangle = \frac{1}{\sqrt{3}}|0\rangle + i\sqrt{\frac{2}{3}}|1\rangle$ in the standard basis, what happens, and with what probability? What about if you measure using the basis $\{| \rightarrow \rangle, | \leftarrow \rangle\}$?
- 2. If you have two qubits states $|\psi\rangle$ and $|\phi\rangle$ such that $\langle\psi|\phi\rangle = 0$, explain what measurement you should use to perfectly distinguish between these two states?
- 3. Explain what will happen in the following situations using bra and ket notation, and the language of collapse:
 - (a) Alice prepares a right diagonal photon, and Bob measures it using a vertically polarized filter.
 - (b) Alice prepares a left diagonal photon, and Bob measures it using a right diagonally polarized filter.