Goals:

- Translate quantified predicates
- Apply de Morgan's rules

No sets on quiz. Quiz available after class.

## LUNCH TODAY: WHAT I DID THIS SUMMER!

## $(m \mid n \equiv m$ divides $n)(M(x, y) \equiv x$ is $y$ 's parent, $S$ is set of all people)

- $B(g) \equiv g$ has a factor greater than 10.


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- $B(g) \equiv g$ has a factor greater than 10.
$\exists t \in \mathbb{N}: t \mid g \wedge t>10$
$(m \mid n \equiv m$ divides $n)(M(x, y) \equiv x$ is $y$ 's parent, $S$ is set of all people)
- $R(r, p) \equiv$ every natural number less than $r$ divides $p$
- $W(a, b) \equiv a$ and $b$ have the same parent
- Hint: Use $M$
- $K \equiv$ every person who has a sibling or half sibling also has a child
- Hint: Use W
- $R(r, p) \equiv$ every natural number less than $r$ divides $p$
$\cdot \forall k \in \mathbb{N}, k<r \rightarrow k \mid p$
- $W(a, b) \equiv \mathrm{a}$ and b both have the same parent
$\cdot \exists p \in S: M(p, a) \wedge M(p, b)$
- $K \equiv$ every person who has a sibling or half sibling also has a child
- Hint: Use $W$
- $\forall x \in S,(\exists y \in S: x \neq y \wedge W(x, y)) \rightarrow$

$$
(\exists w \in S: M(x, w)
$$

