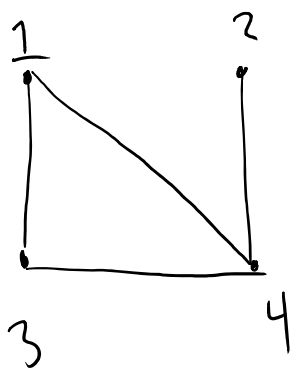


Ways to Represent Graphs in Computer

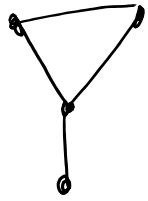
Adjacency Matrix

	1	2	3	4
1	0	0	1	1
2	0	0	0	1
3	1	0	0	1
4	1	1	1	0



Store as array A in memory. Can learn $A[i,j]$ in $O(1)$ time.

Which adjacency matrix represents this graph?



0	1	0	0
1	0	1	1
0	1	0	1
0	1	1	0

A

0	1	1	1
1	0	0	0
1	0	1	0
1	0	0	0

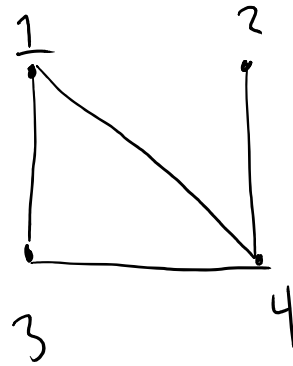
B

0	1	0	0
1	0	1	0
0	1	0	1
0	0	1	0

C

Adjacency List

Vertex	Adjacent Vertices
1	3, 4
2	4
3	1, 4
4	1, 2, 3



Store as an array of lists

Can access $A[3]$, (the list) in $O(1)$ time, but

then to go through list takes time $O(L)$ where L is length of list. Can learn $A[3].length$ in $O(1)$ time.

Edge List

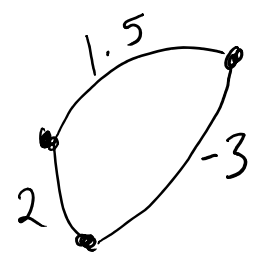
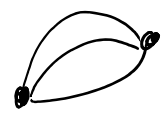
Can represent graph as list of edges, but worstcase time complexity bad for most applications

def: The degree of a vertex is the number of adjacent edges.

def: A vertex v_1 is adjacent to vertex v_2 if connected by an edge

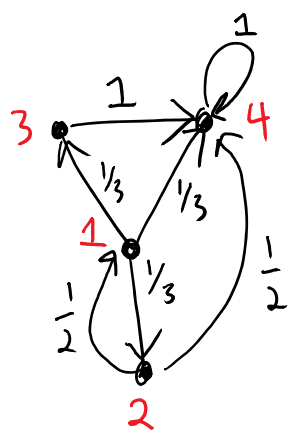
How would you represent a

- directed graph?
- graph with self-loops?
- graph with multi edges?
- graph with weighted edges?



Using Adjacency Matrix / Adjacency List?

Give representations of this graph using both approaches:



	1	2	3	4
1	0	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
2	$\frac{1}{2}$	0	0	$\frac{1}{2}$
3	0	0	0	1
4	0	0	0	1

v	List
1	$(2, \frac{1}{3}), (3, \frac{1}{3}), (4, \frac{1}{3})$
2	$(1, \frac{1}{2}), (4, \frac{1}{2})$
3	$(4, 1)$
4	$(4, 1)$